

Preliminary MD Results on:

Continuous Beta-Beat Measurements -

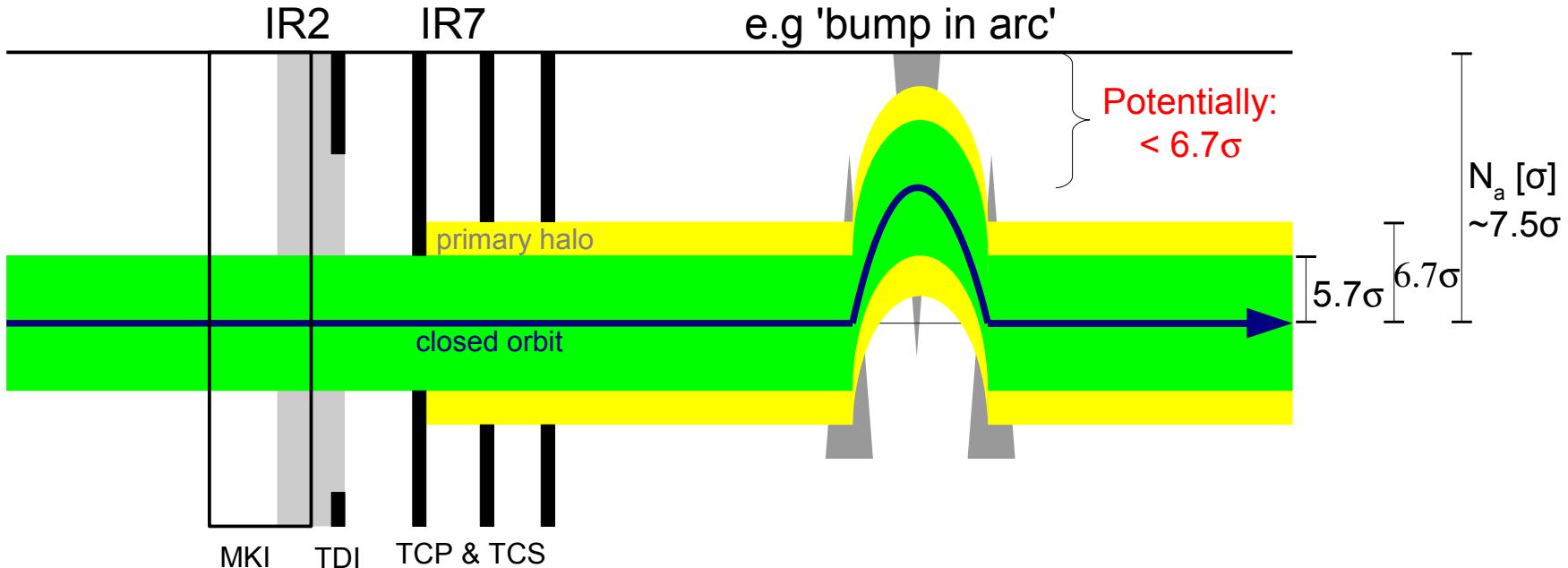
Prototype Tests at the SPS

**A. Boccardi, E. Calvo Giraldo, M. Gasior,
J.L. Gonzales, R.Jones, R.J. Steinhagen**

Accelerator and Beams Department
Beam Instrumentation Group

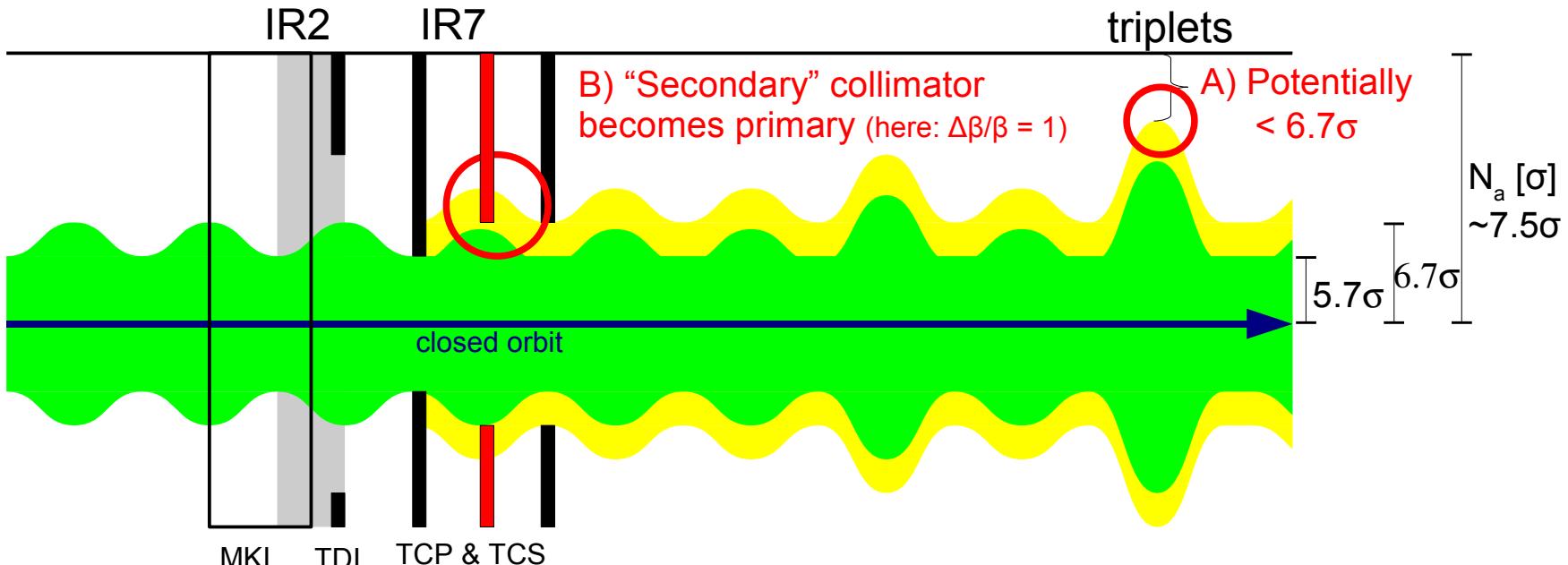
- Motivation: System dependence on known/constant beta-function:
 - Machine Protection and Collimation, Physics, Squeeze Diagnostics
 - Classic methods: 'kick'-type excitation & BPMs, K-modulation & Q-PLL, Closed-orbit-response (LOCO)
 - cannot achieve the required precision/time-scales under nominal conditions!
- β -Phase Advance Method
 - BBQ based Test-Setup in SPS LSS5
 - Systematic and statistical noise contribution
 - Exploitation Examples: SPS lattice drifts & off-momentum beta-beat
- Next Steps & Control of Betatron-Function:

- Combined failure: Local orbit bump and collimation efficiency (/kicker failure):



- Primary collimator (TCP) limits $|x_\beta(s)|_{\max}$ locally to $< 5.7\sigma$, secondary collimator (TCS) at $\sim 6.7\sigma$
 - To guarantee two stage cleaning efficiency/machine protection:
 - Local: TCP must be $> 0.7\sigma$ closer than TCS w.r.t. the beam \rightarrow Orbit FB
 - Global: no other object (except TCP) closer to beam than TCS
- \rightarrow Orbit bumps may compromise function of machine protection/collimation
- \rightarrow tackled by LHC Orbit Feedback

- Combined failure: beta-beat and collimation efficiency



- "Collimator gap must be **10 times smaller** than available triplet aperture!"¹

$$a_{coll} \leq a_{triplet} \cdot \sqrt{\frac{\beta_{coll}}{\beta_{triplet}}} \cdot \left(\frac{A_{primary}^{max}}{A_{secondary}^{max}} \right)$$

~ 0.15 ~ 0.6

- A) β -Beat reduces required protection: $\Delta\beta/\beta \approx 20\% \rightarrow 20\%$ tighter collimator settings
- B) β -Beat reduces cleaning performance

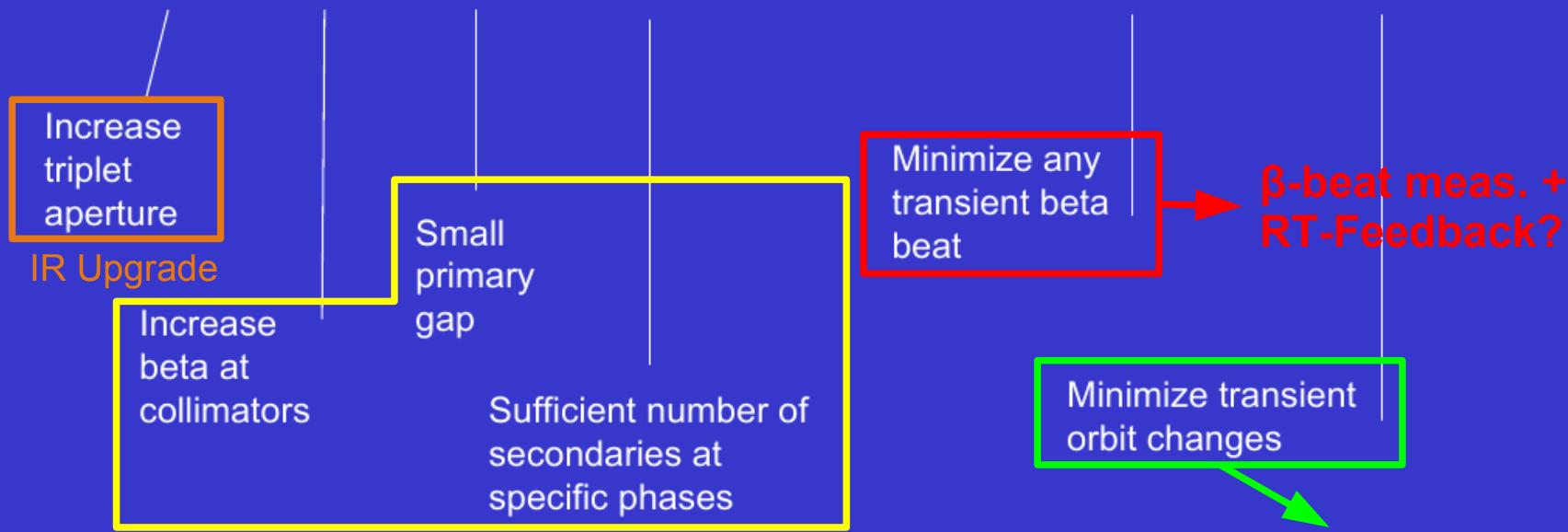
¹ R. Assmann, "Collimation and Cleaning: Could this limit the LHC Performance?", Chamonix XII, 2003

Performance Limitations & Constraints on β^*

If retraction is adjusted such to allow some maximum transient beta beat and orbit error, then **constraint of β^* :**

$$\text{N.B. } C = \beta_{\text{trip}} \cdot \beta^*$$

$$\beta^* \geq \frac{C^2}{a_{\text{triplet}}^2 \cdot \beta_{\text{coll}}} \cdot \left(n_{\text{prim}} + \Delta A_{\max} + 1.7 \cdot \left[n_{\text{prim}} \cdot \sqrt{\frac{\Delta \beta_{\max}}{\beta_0}} + \frac{\Delta x_{\text{orbit}}^{\max}}{\sigma_x} \right] \right)^2$$



Larger β^* - A way to relax operational collimator tolerances!

(However, loose passive protection)

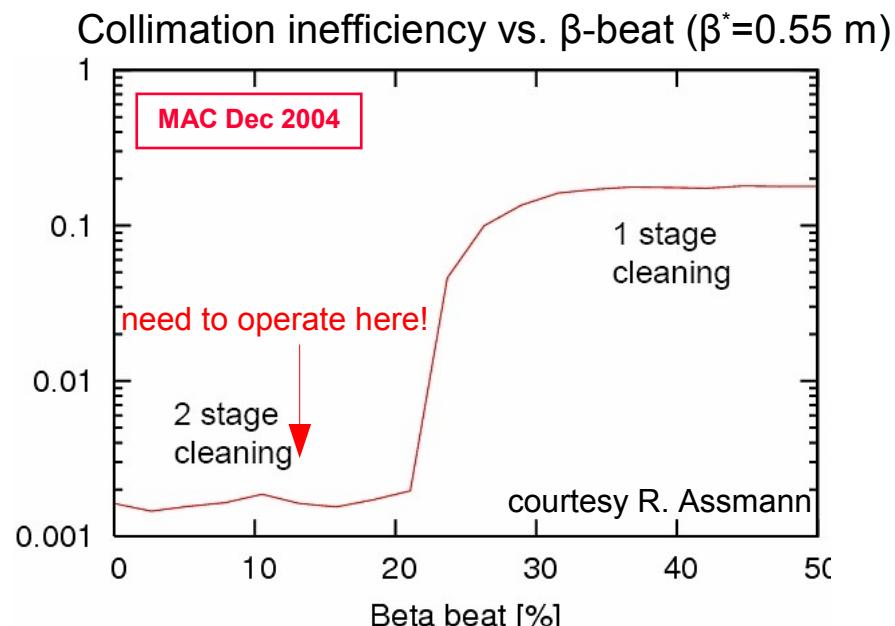
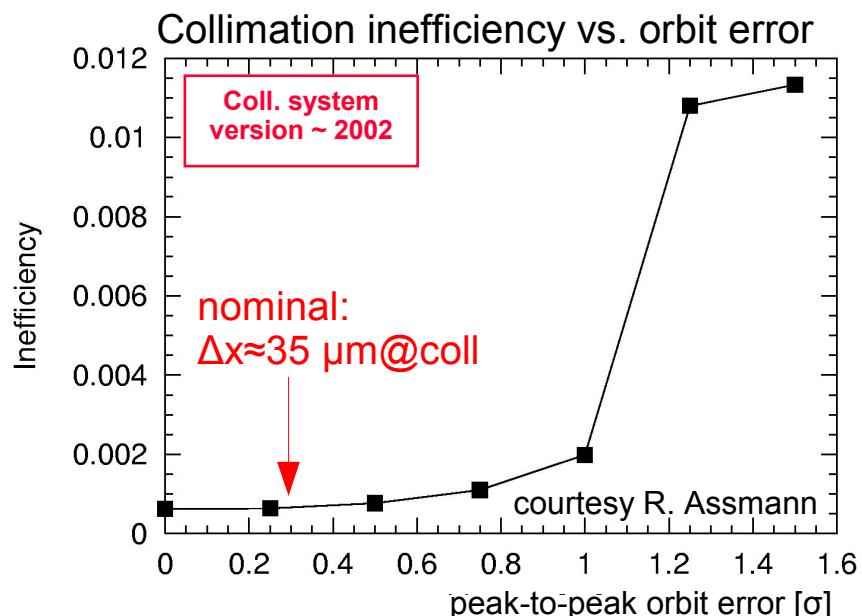
- Maximum allowed safe beam intensity^{1,2}:

$$N_{max} \leq \frac{\tau_{min} \cdot R_q \cdot L_{dil.}}{\eta}$$

- Min. accept. lifetime: $T_{min} \approx 10$ min.
- Dilution length: $L_{dil} \approx 50$ m
- Quench level (@7 TeV) R_q : $R_q \approx 7.6 \cdot 10^6$ prot./m/s
- Collimation inefficiency: η

Peak-Luminosity:

$$L_{max} \approx \frac{1}{4\pi} \cdot \frac{N_{max} \cdot n_b f_{rev}}{\beta^* \epsilon}$$

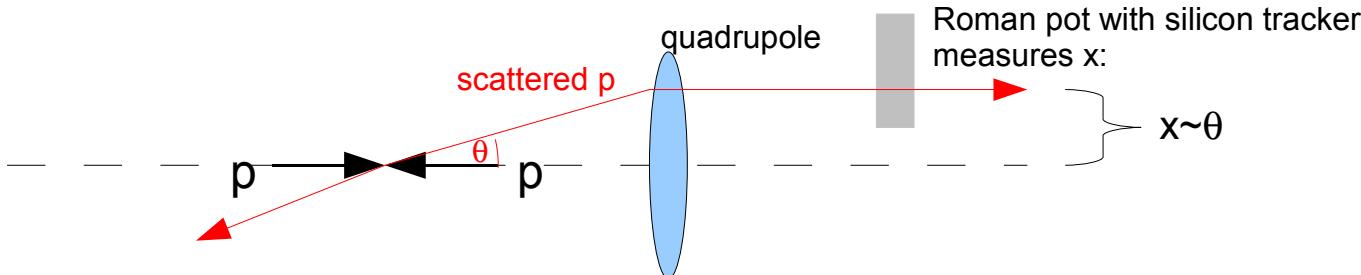


¹ R. Assmann, "Collimation and Cleaning: Could this limit the LHC Performance?", Chamonix XII, 2003

² S. Redaelli, "LHC aperture and commissioning of the Collimation System", Chamonix XIV, 2005

³ R. Steinhagen, "Closed Orbit and Protection", MPWG #53, 2005-12-16

- Special parallel to point focusing machine optic ($\beta_0 \approx 1600$ m)



- Roman Pots move close to the beam halo, measure dN/dt down to:

$$t_{min} = (p \theta_{min})^2 \sim \frac{p^2}{\beta_0 \beta_d} \cdot x_{min}^2$$

- Observables: abs. Luminosity, total p-p cross-section, diffractive physics
 - Requires good knowledge on
 - Beta-functions β_0 at IP and β_d at detector
 - Beam momentum p
 - minimum distance of roman pot x_{min} w.r.t. beam centre
- Desired: $\Delta L/L \approx 1\% \rightarrow \Delta t/t \approx 1\% \rightarrow 0.5 \cdot \Delta \theta/\theta \approx \Delta x/x \approx 5 \cdot 10^{-3}$
 - absolute beam position stability at roman pot ($x_{min} \sim 1\text{mm}$) $< 5 \mu\text{m}!!$
 - value of betatron function at IP and RP: $\rightarrow \Delta \beta/\beta \approx 1\% !!$

Limitations on Squeeze Diagnostic

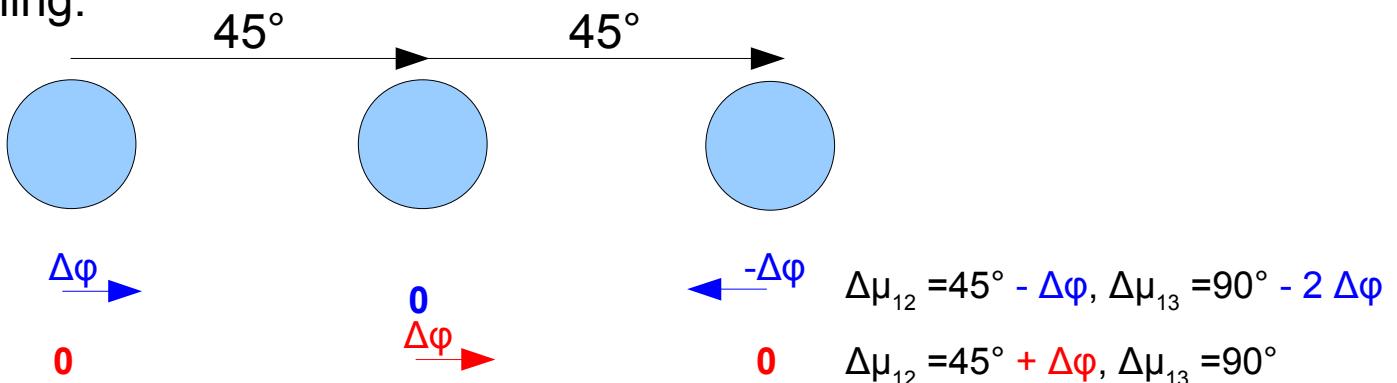
- Squeeze involves > 45 individual magnetic strength settings (Optics), so far:
no continuous check on effective optics during/at the end of individual steps
- “Classic” methods may not reach/be compatible with nominal requirements
 - K-modulation induced Q-Changes:
$$\Delta Q \approx \frac{1}{4\pi} \cdot \beta(s) \cdot \Delta k(s)$$
 - Limit: knowledge on quadrupole transfer function (hysteresis, D&S, $\beta|^{max} \approx 4.2\text{km}$ & $\Delta Q^{max} < 10^{-3} \rightarrow \Delta k/k_{nom} < 5 \cdot 10^{-5}$)
 - Kick + turn-by-turn analysis of BPM (phase and/or amplitude), limits:
 - Potential particle loss (beta-functions at triplet) & emittance blow-up
 - **Systematic phase errors, amplitude detuning/Landau damping**
 - large kicks may probe phase advances (dynamic aperture) which may not be relevant for nominal beam operation/parameters
 - beam will be collimated at 6 sigma (kick amplitudes < 1.2 mm @7TeV)!
 - ... not ideal for continuous monitoring/regular operation.
 - Closed orbit response analysis (LOCO):
 - resolution/performance compatible with nominal operation
 - Limit: scan requires several minutes per IP (full scan: ~2 OP-shifts)

- Long history at CERN. Original idea dates back to AB-BI report (doctoral thesis)
P.Castro, *Luminosity and Betatron Function Measurement at [...] LEP*, CERN SL/96-70 (BI)
- ... beating in amplitude related to beating in phase:

$$\frac{\Delta \beta}{\beta}(s) = \frac{1}{2 \sin(2\pi Q)} \oint \beta_k \cos(2 \cdot |\mu(s) - \mu(a)| - 2\pi Q) \Delta k(a) da$$

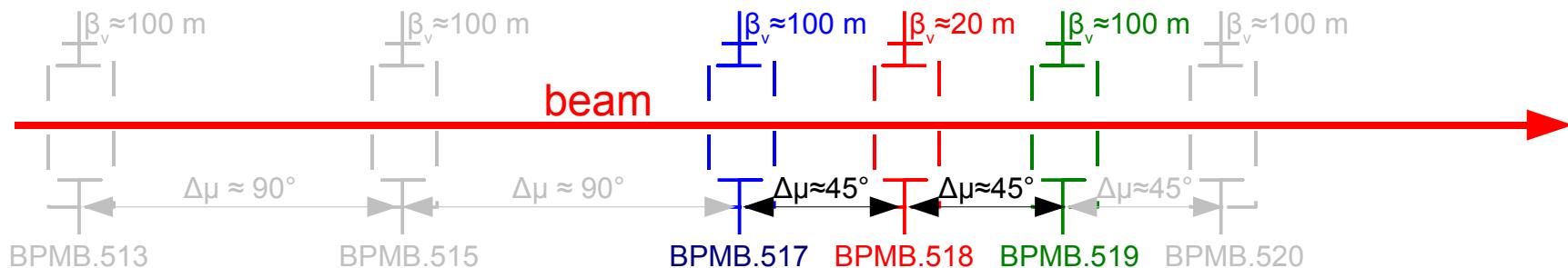
$$\mu(s) := \int_0^s \frac{1}{\beta(a)} da \quad \longrightarrow \quad \frac{\Delta \mu}{\mu}(s) \sim \frac{\Delta \beta}{\beta}(s)$$

- Phase sampling:

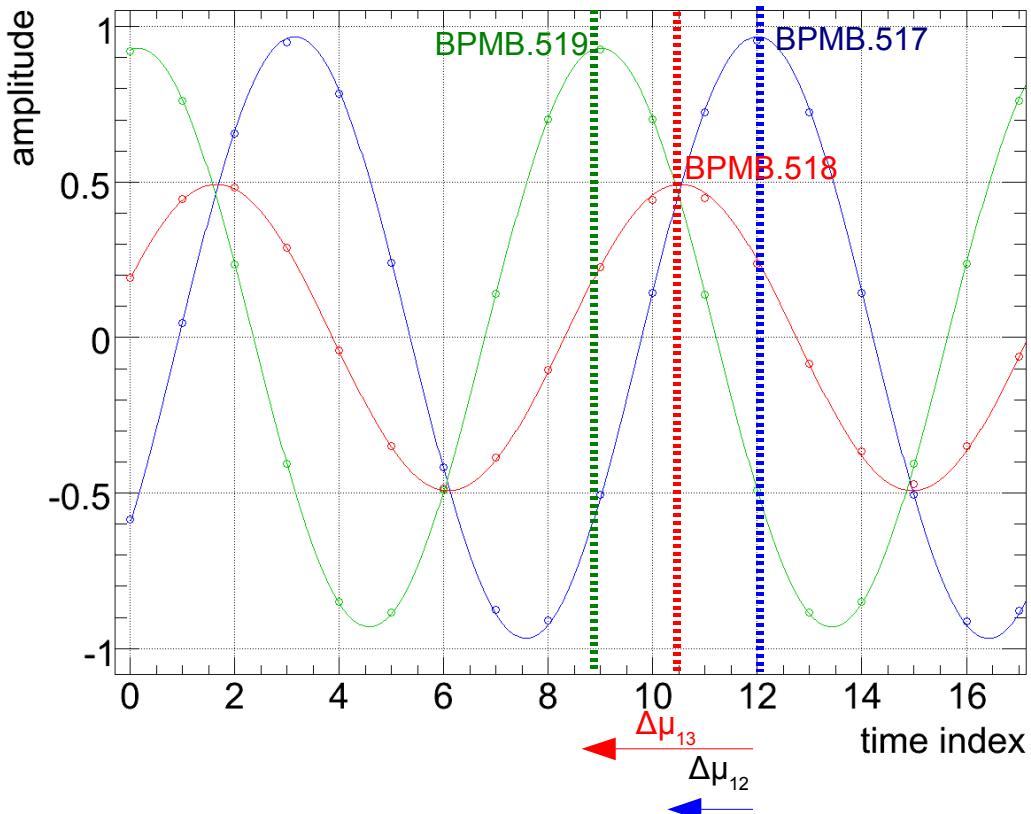


- Beta-Beat reconstruction (FB/Control would work with phases):

$$\frac{\Delta \beta_1}{\beta_1} = \frac{\cot(\Delta \mu_{12}^{meas.}) - \cot(\Delta \mu_{13}^{meas.})}{\cot(\Delta \mu_{12}^{theo.}) - \cot(\Delta \mu_{13}^{theo.})} \quad \frac{\Delta \beta_2}{\beta_2} = \frac{\cot(\Delta \mu_{12}^{meas.}) - \cot(\Delta \mu_{23}^{meas.})}{\cot(\Delta \mu_{12}^{theo.}) - \cot(\Delta \mu_{23}^{theo.})} \quad \frac{\Delta \beta_3}{\beta_3} = \frac{\cot(\Delta \mu_{23}^{meas.}) - \cot(\Delta \mu_{13}^{meas.})}{\cot(\Delta \mu_{23}^{theo.}) - \cot(\Delta \mu_{13}^{theo.})}$$



- Measurement (markers), sinusoidal fit (solid line):

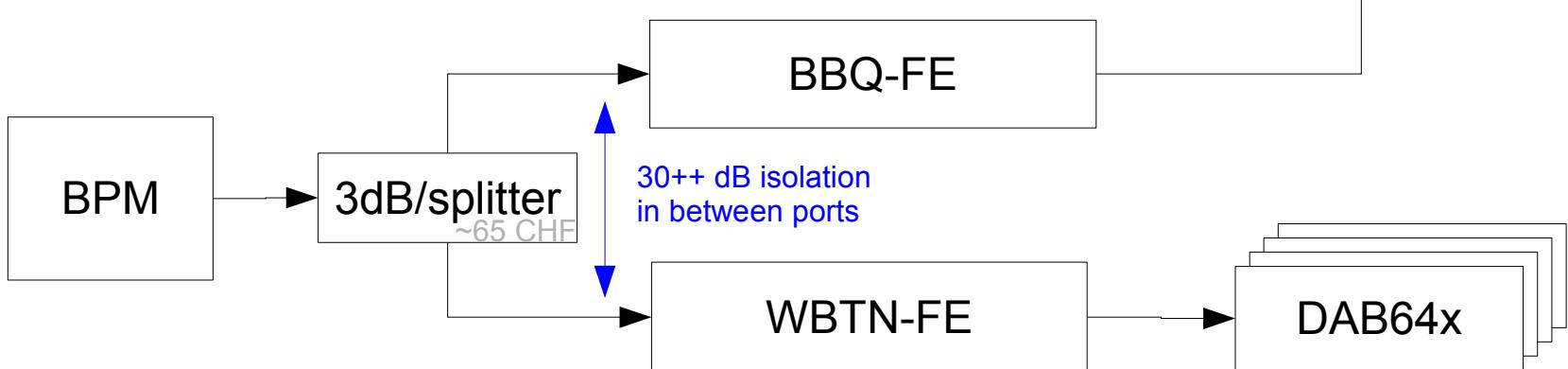


$$\frac{\Delta \beta_1}{\beta_1} = \frac{\cot(\Delta \mu_{12}^{meas.}) - \cot(\Delta \mu_{13}^{meas.})}{\cot(\Delta \mu_{12}^{theo.}) - \cot(\Delta \mu_{13}^{theo.})}$$

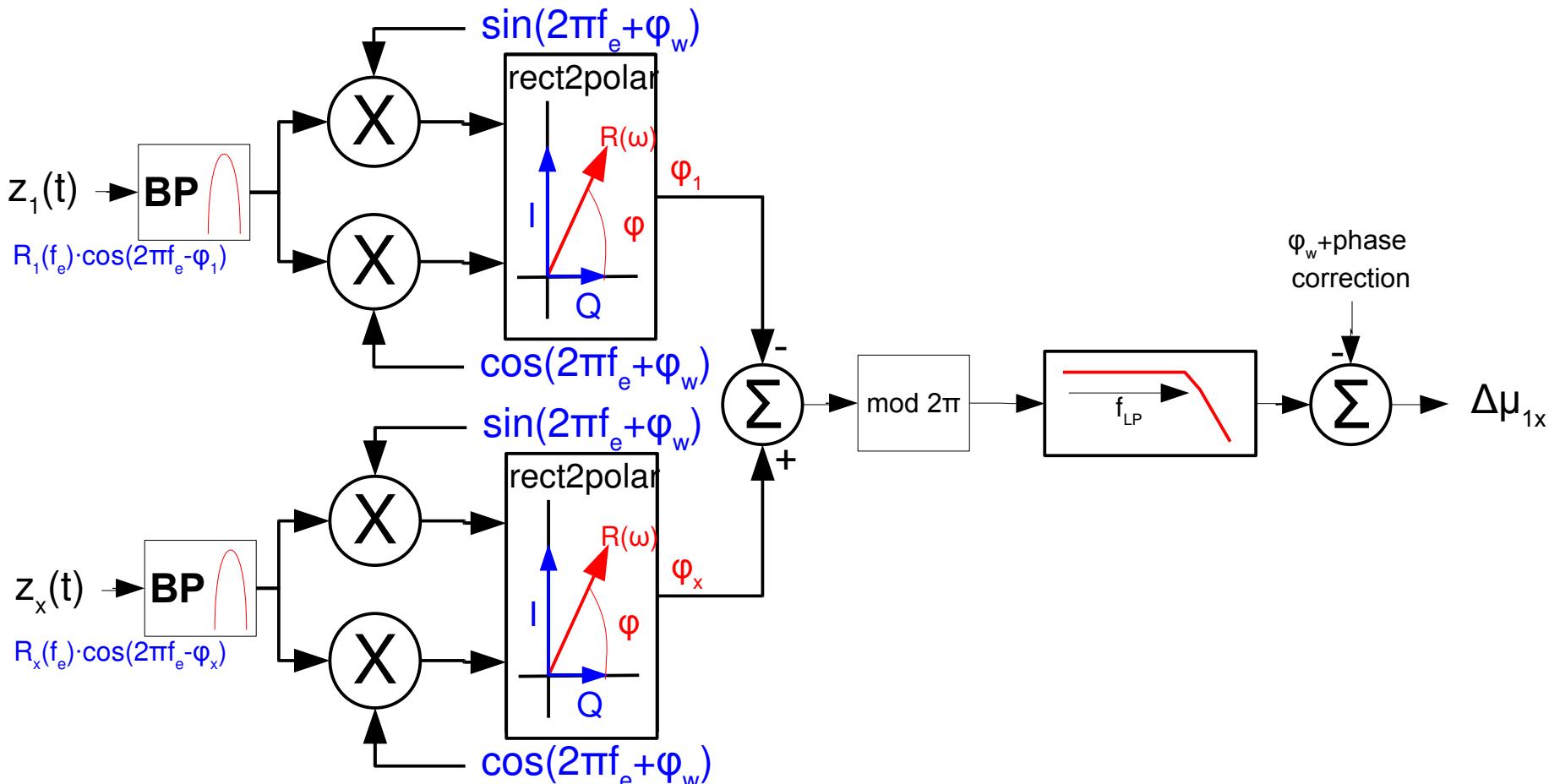
$$\frac{\Delta \beta_2}{\beta_2} = \frac{\cot(\Delta \mu_{12}^{meas.}) - \cot(\Delta \mu_{23}^{meas.})}{\cot(\Delta \mu_{12}^{theo.}) - \cot(\Delta \mu_{23}^{theo.})}$$

$$\frac{\Delta \beta_3}{\beta_3} = \frac{\cot(\Delta \mu_{23}^{meas.}) - \cot(\Delta \mu_{13}^{meas.})}{\cot(\Delta \mu_{23}^{theo.}) - \cot(\Delta \mu_{13}^{theo.})}$$

- Yet another exploitation of the BBQ Principle:
 - AC-coupled peak detector:
 - no saturation, self-triggered, no gain changes between pilot and nominal
 - intrinsically down samples spectra: ... 6 GHz → 1kHz ... f_{rev}
 - Base-band operation: very high sensitivity/resolution ADC available
 - Measured resolution estimate: < 10 nm
→ ε blow-up is a non-issue
- Digital acquisition: HP Proliant 16", 1U + M-AUDIO Delta 1010
 - 8 analogue inputs/outputs, 16", 1U
 - frequency response: 20Hz-22kHz, +/-0.3dB
 - >100 dB dynamic range/S/N ratio
 - THD: 0.00072% (A/D), 0.00200% (D/A)

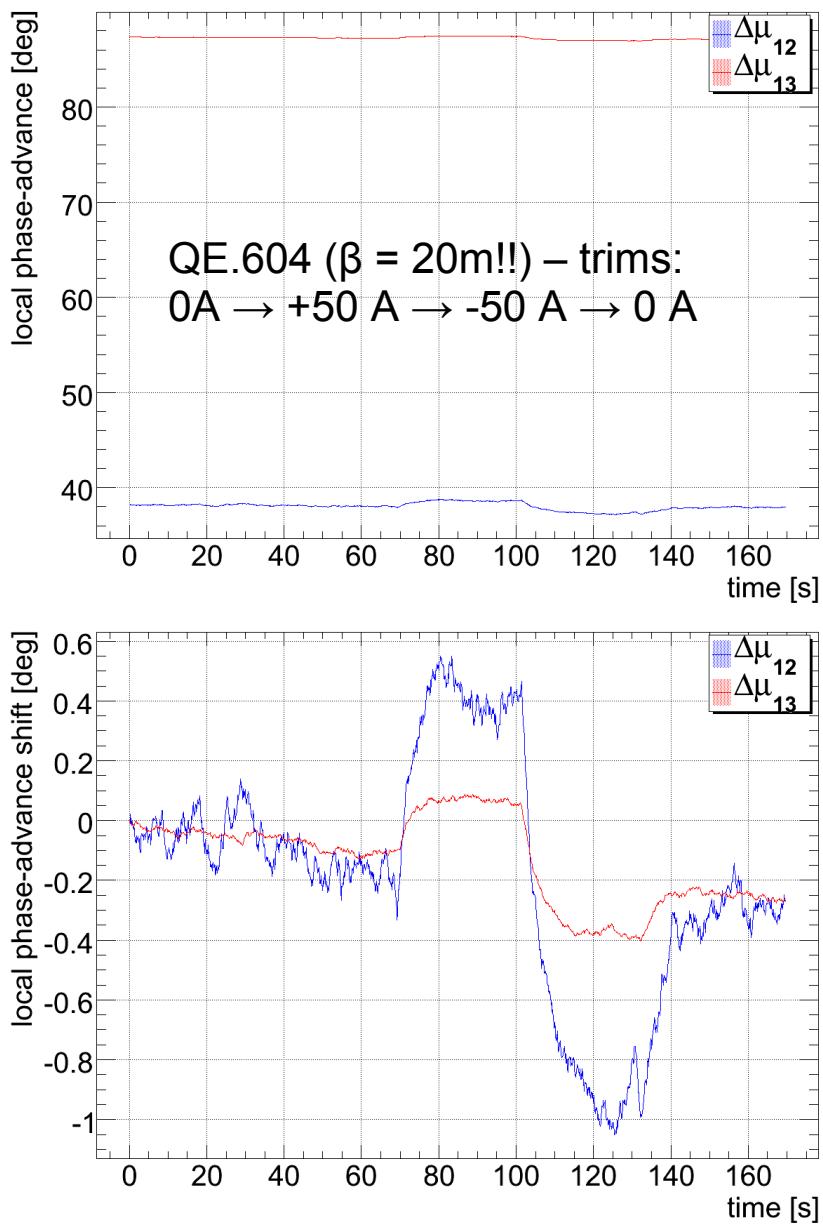
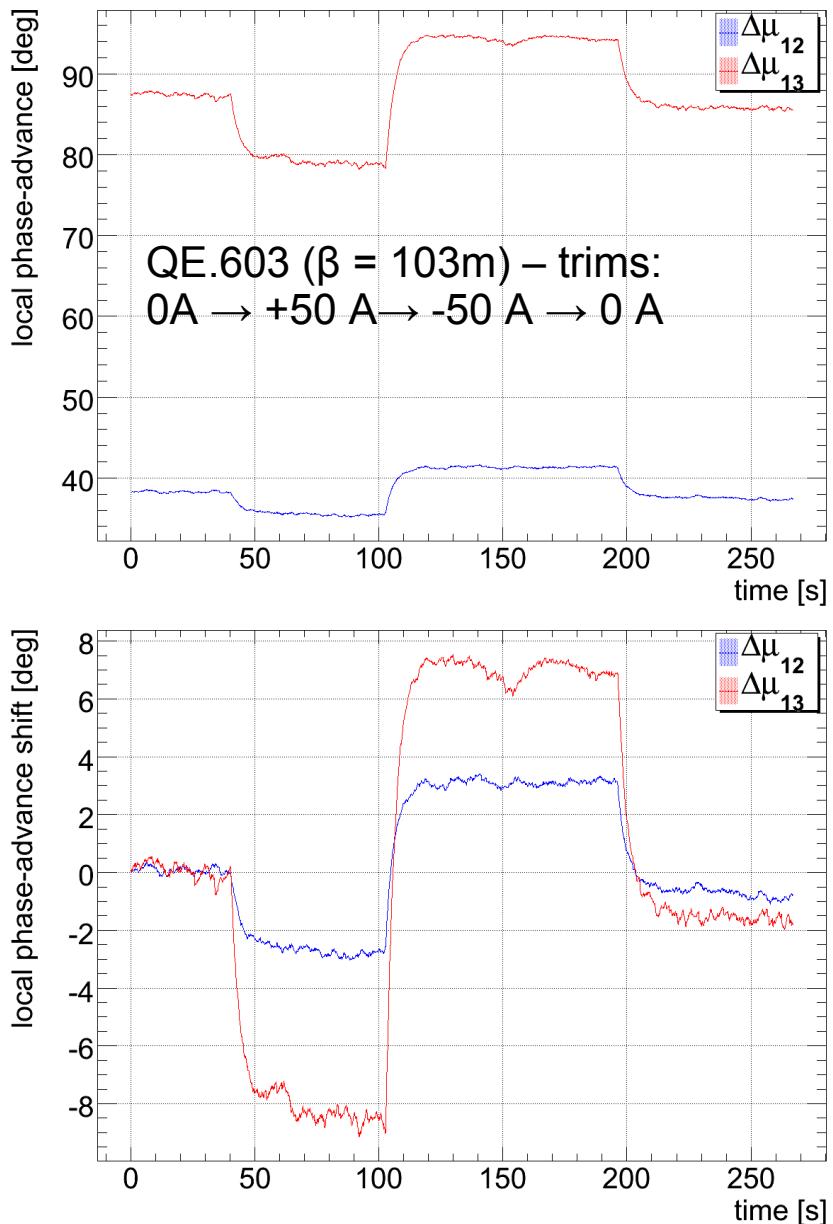


- Modified mixing scheme:



- Alternative method to mixing: IIR Hilbert transformer

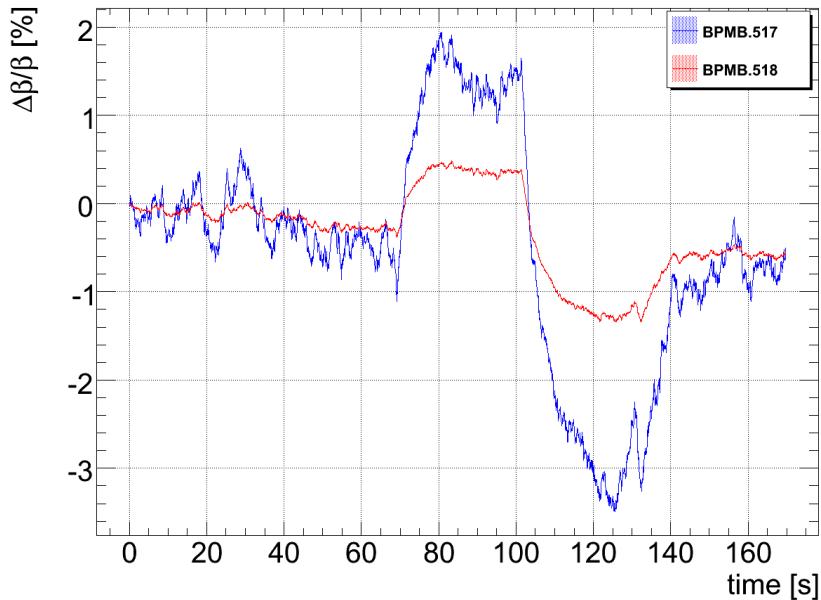
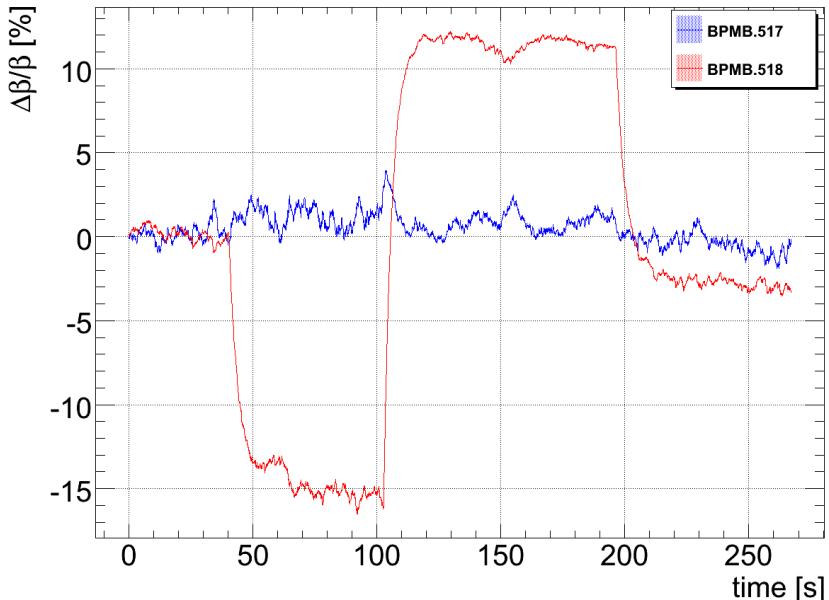
QE.603/QE.604 induced β -Phase-Advance Beating



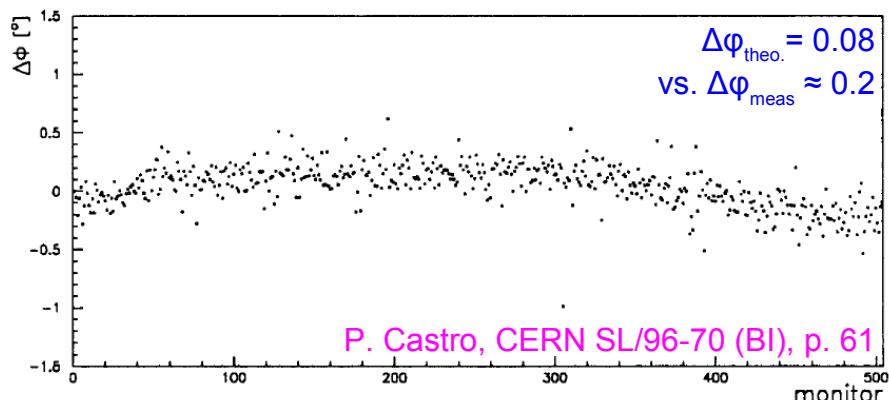
QE.603/QE.604 induced β -Beating

- Corresponding beta-beat:

$$\frac{\Delta \beta}{\beta} = \frac{\cot(\Delta \mu_{12}^{meas.}) - \cot(\Delta \mu_{13}^{meas.})}{\cot(\Delta \mu_{12}^{theo.}) - \cot(\Delta \mu_{13}^{theo.})}$$



- Measured beta-beat is compatible with magnet calibration curves.
- Peak-to-peak β -beat “noise”: ~ 0.5 %
 - unlikely due to diagnostic
 - seen already at LEP:
(though not time resolved)
 - real drift of the optics!



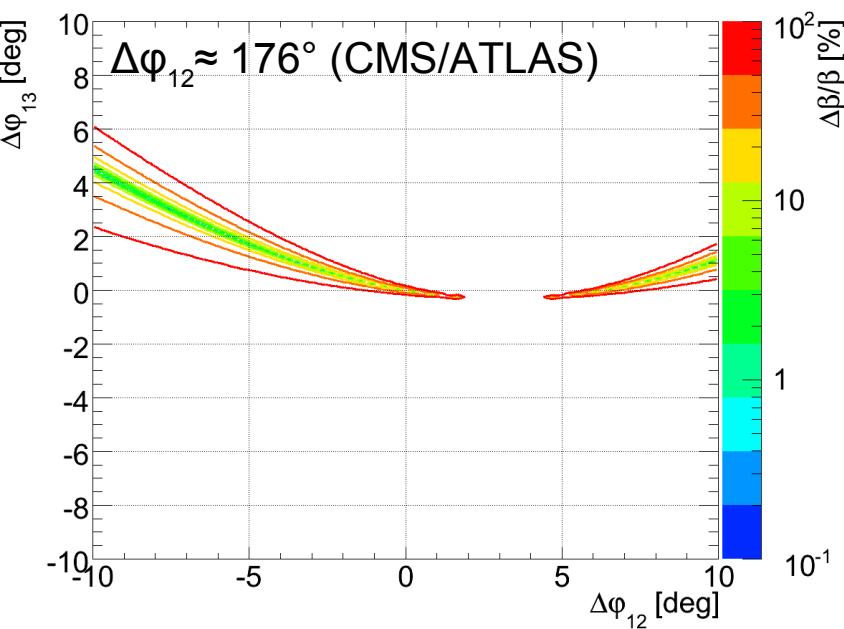
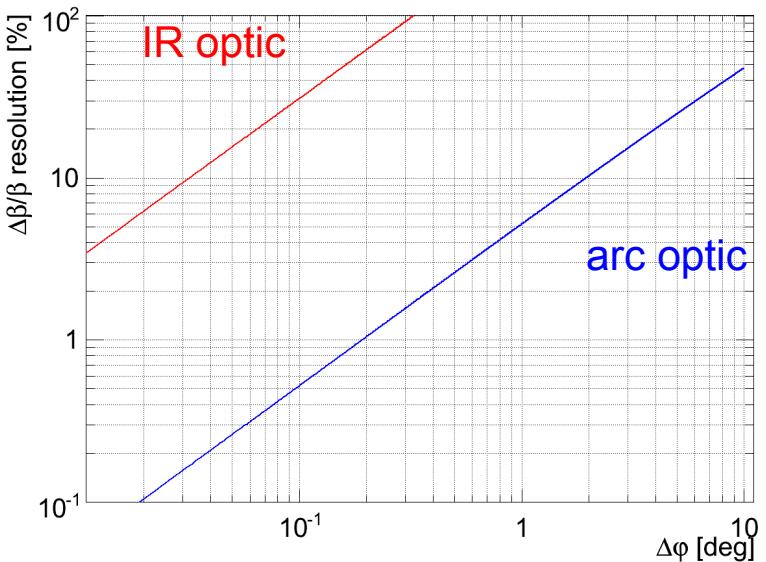
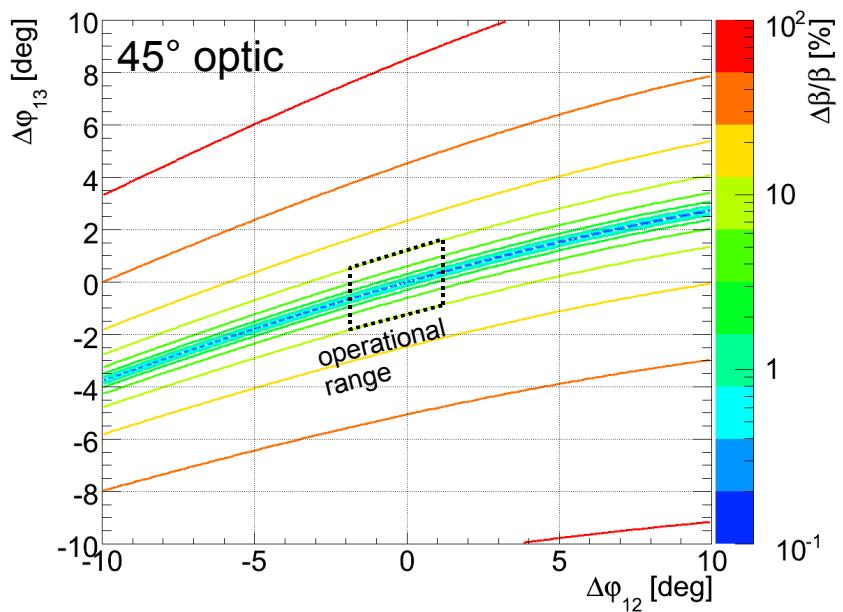
- Residual resolution/systematic error

$$\frac{\Delta \beta_1}{\beta_1} = \frac{\cot(\Delta \mu_{12}^{meas.}) - \cot(\Delta \mu_{13}^{meas.})}{\cot(\Delta \mu_{12}^{theo.}) - \cot(\Delta \mu_{13}^{theo.})}$$

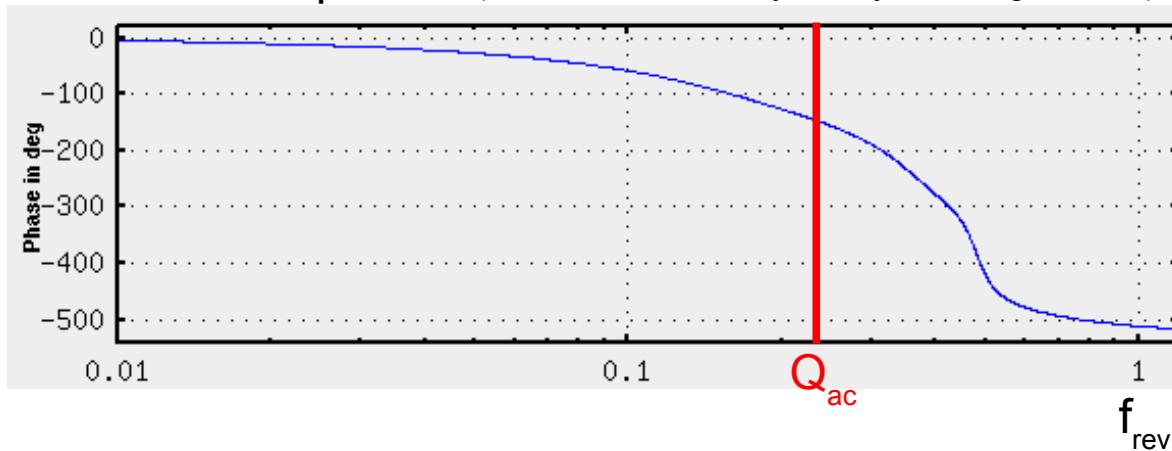
$$\Delta \mu_{1i}^{meas.} := \Delta \mu_{1i}^{theo.} + \Delta \varphi_{1i}$$

- ARC optics: requires error below $\sim 1^\circ$
- IP optics: requires error below $\sim 0.02^\circ$

N.B. Plots have logarithmic z-scale!



- Sources – usually depend on observation/excitation frequency
 - Systematic delays: $\Delta\varphi [deg] = 360^\circ \cdot \Delta\tau f$
 - Pick-up to acquisition system cable length (e.g. 100 m@ $Q_{AC} = 0.25 f_{rev}$)
 - SPS: $\Delta\varphi \approx 2^\circ$ LHC $\Delta\varphi \approx 0.5^\circ$: $\Delta\beta/\beta_{sys} \approx 3\text{-}10\%$ (45° lattice)
 - cable delay compensation mandatory for direct β^* -Measurements
 - Low-frequency pre-processing and analogue front-end asymmetry (mostly filters, N.B. Current has been not optimised for those issues)
 - Delta 1010 – analogue pre-filter: $\Delta\varphi \approx 7^\circ$ (measured)
 - BBQ front-end: $\Delta\varphi \approx 10^\circ$ (measured, here: only Chebychev stage shown)



- Systematic drift: $< 0.1^\circ \rightarrow$ will be further reduced

Beta-Beat Measurement Error Sources II/II

Statistical Phase Noise

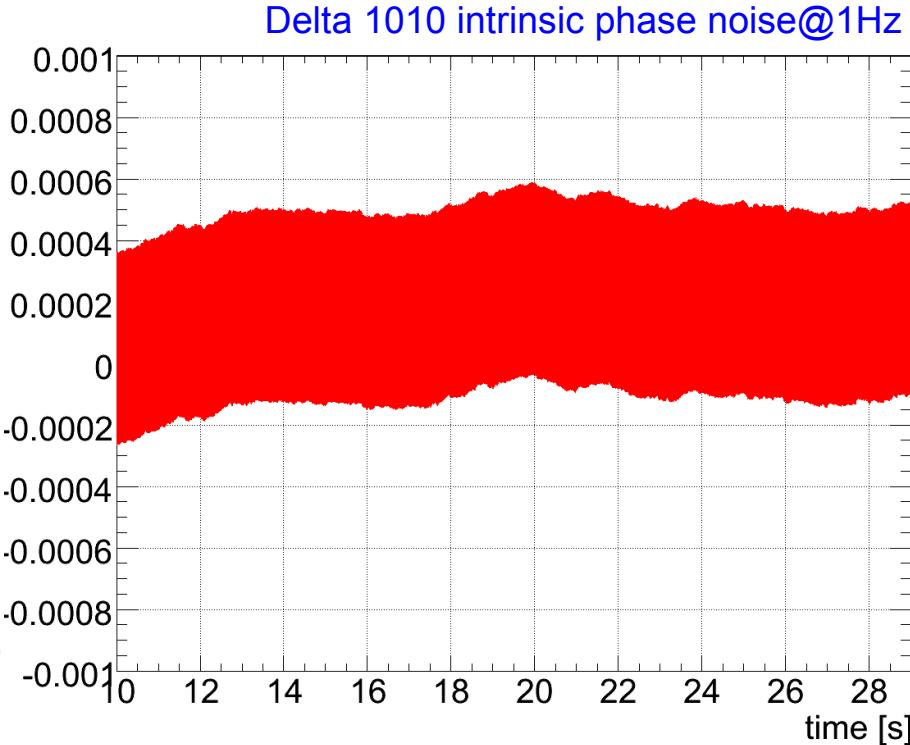
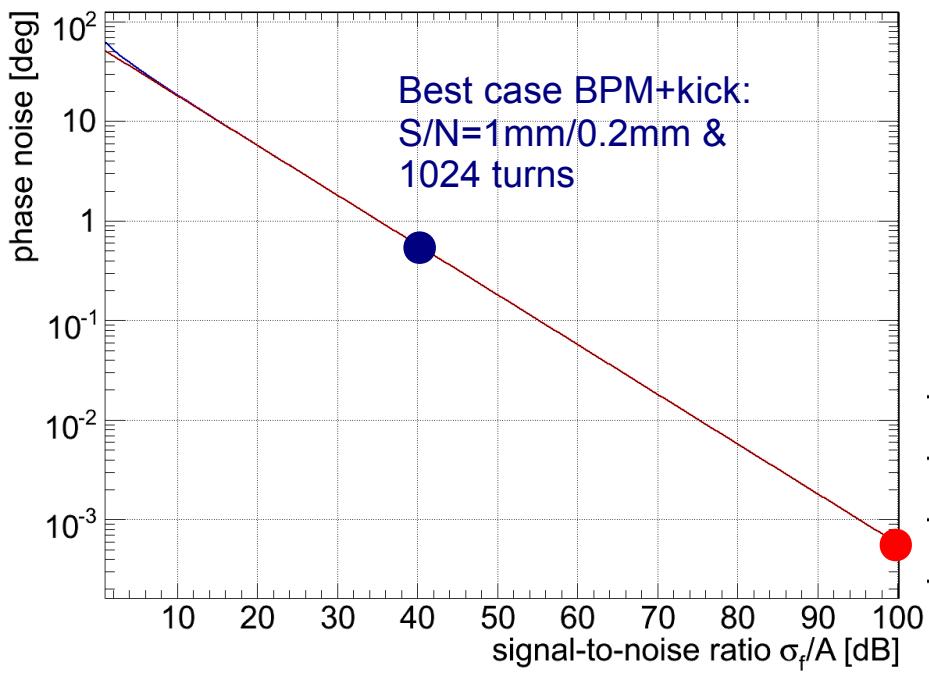
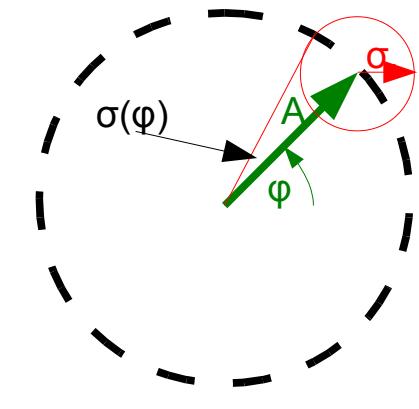
- Statistical noise adds vectorial to the carrier signal:

- excitation amplitude (carrier signal): A
- noise in time (frequency) domain: σ_t (σ_f)
- Equivalent number of turns: N

$$\sigma(\varphi) = \arcsin\left(\frac{\sigma_f}{A}\right) = \arcsin\left(\sqrt{\frac{2}{N}} \frac{\sigma_t}{A}\right)$$

for small noise
to signal ratios

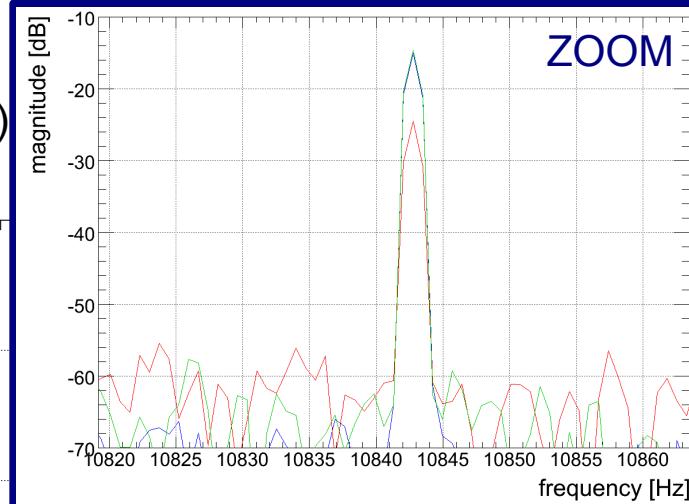
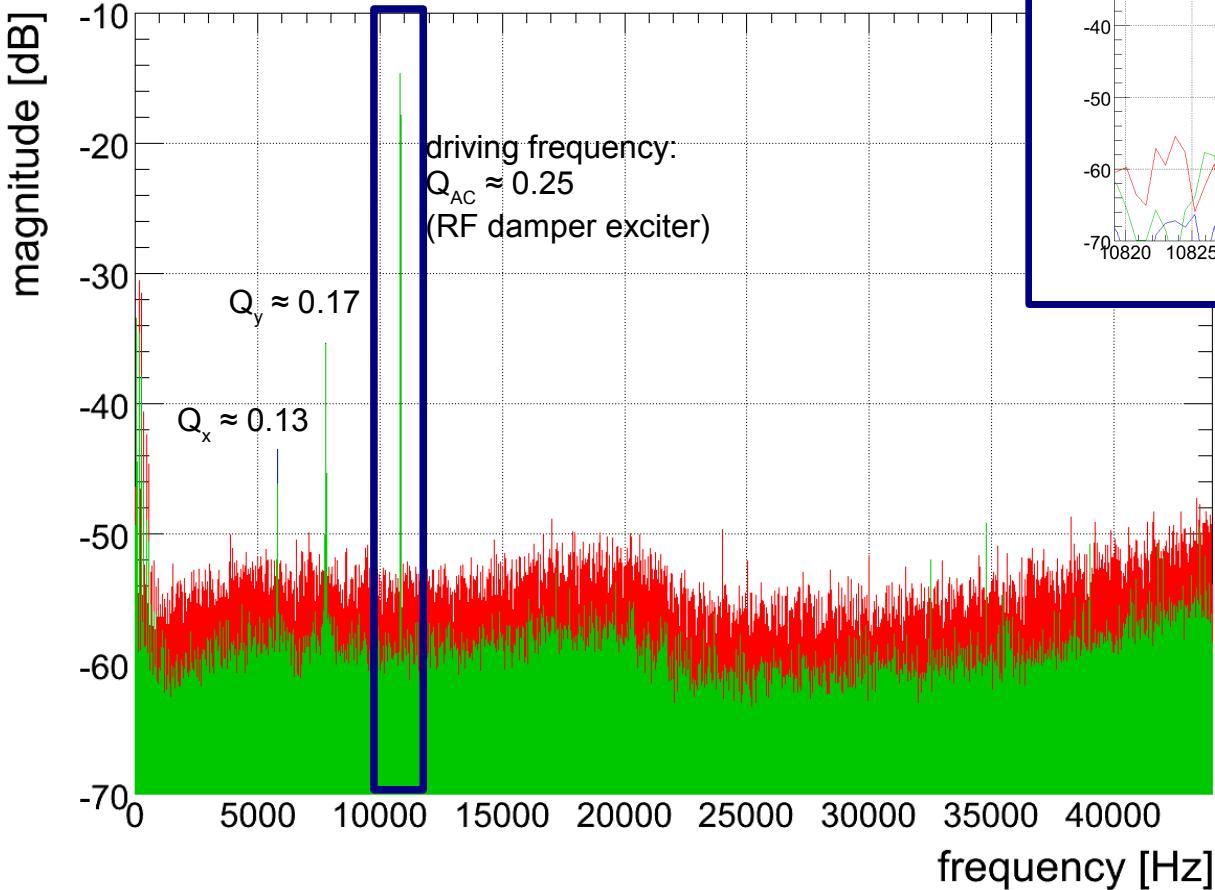
$$\approx \sqrt{\frac{2}{N}} \frac{\sigma_t}{A}$$



Typical SPS Beam Spectrum

single bunch, $\sim 7 \cdot 10^{10}$ protons@270GeV (coasting)

- Based on 128k turns (~ 1.3 seconds)
 - noise floor (time domain): ~ 100 nm (BBQ1: ~ 5 nm)
 - driven 'AC-dipole' signal: $\sim 20\text{-}30$ μm

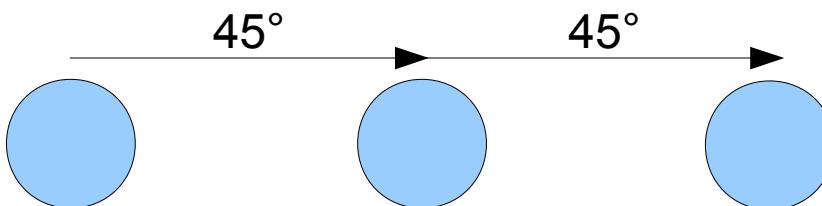
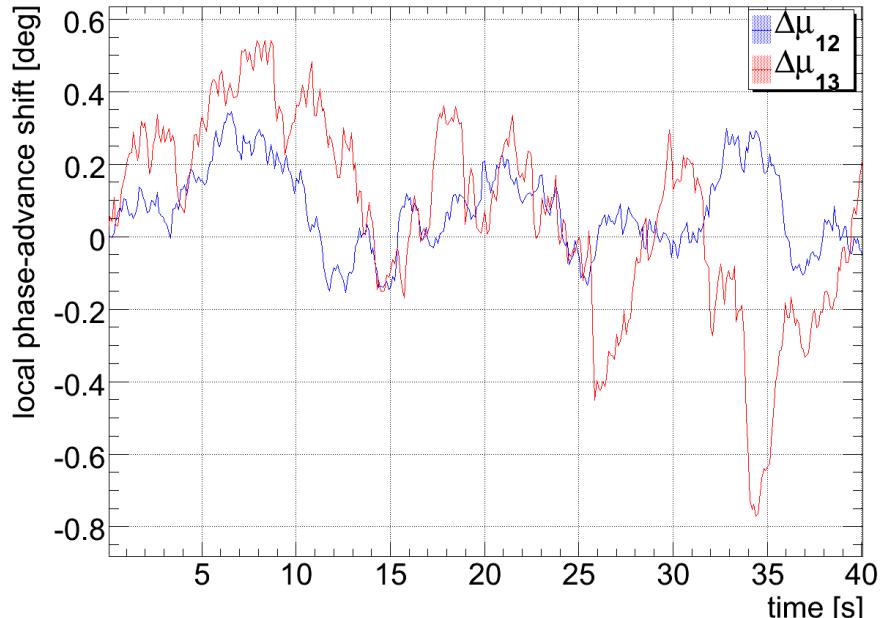


- LHC BPMs give ~ 30 dB less signal than BBQ1 installation (buttons vs. 30 cm strip-line)
- Residual tune signals $\sim 0.5/2$ μm (calibrated w.r.t. Signal seen on SPS BPMs)
- off-resonance excitation \rightarrow no emittance blow-up

Residual Beta-Beat Drifts - Revisited

- Residual phase motion (blue: BPM1->2, red: 0.5*BPM1->3)

- Acquisition/electronic induced noise would be “equal”/randomly distributed over all channels
 - GM induced sextupole shifts
 - $\Delta x \approx 100 \text{ um r.m.s.}$
 $\rightarrow \Delta\beta/\beta \approx 0.1\text{-}0.2\%$
 - bit too large to be the only perturbation source...



Case I: $\Delta\phi$ →

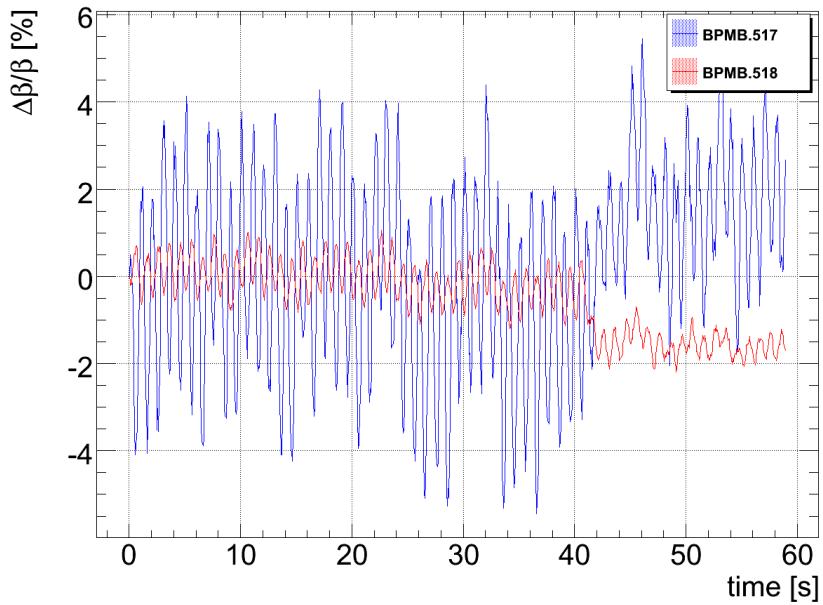
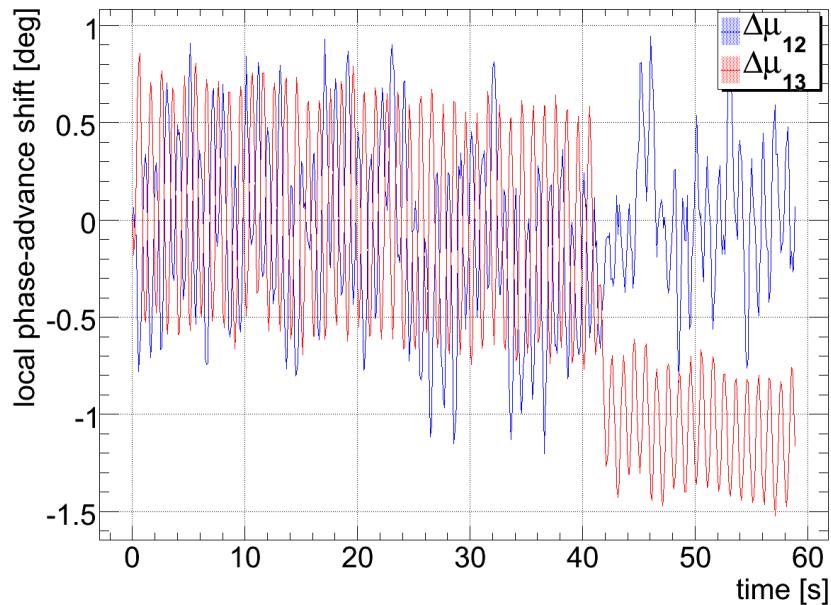
$$\Delta\mu_{12} = 45^\circ - \Delta\phi, \Delta\mu_{12} = 90^\circ - 2\Delta\phi$$

Case II: 0 → $-\Delta\phi$

$$\Delta\mu_{12} = 45^\circ + \Delta\phi, \Delta\mu_{12} = 90^\circ$$

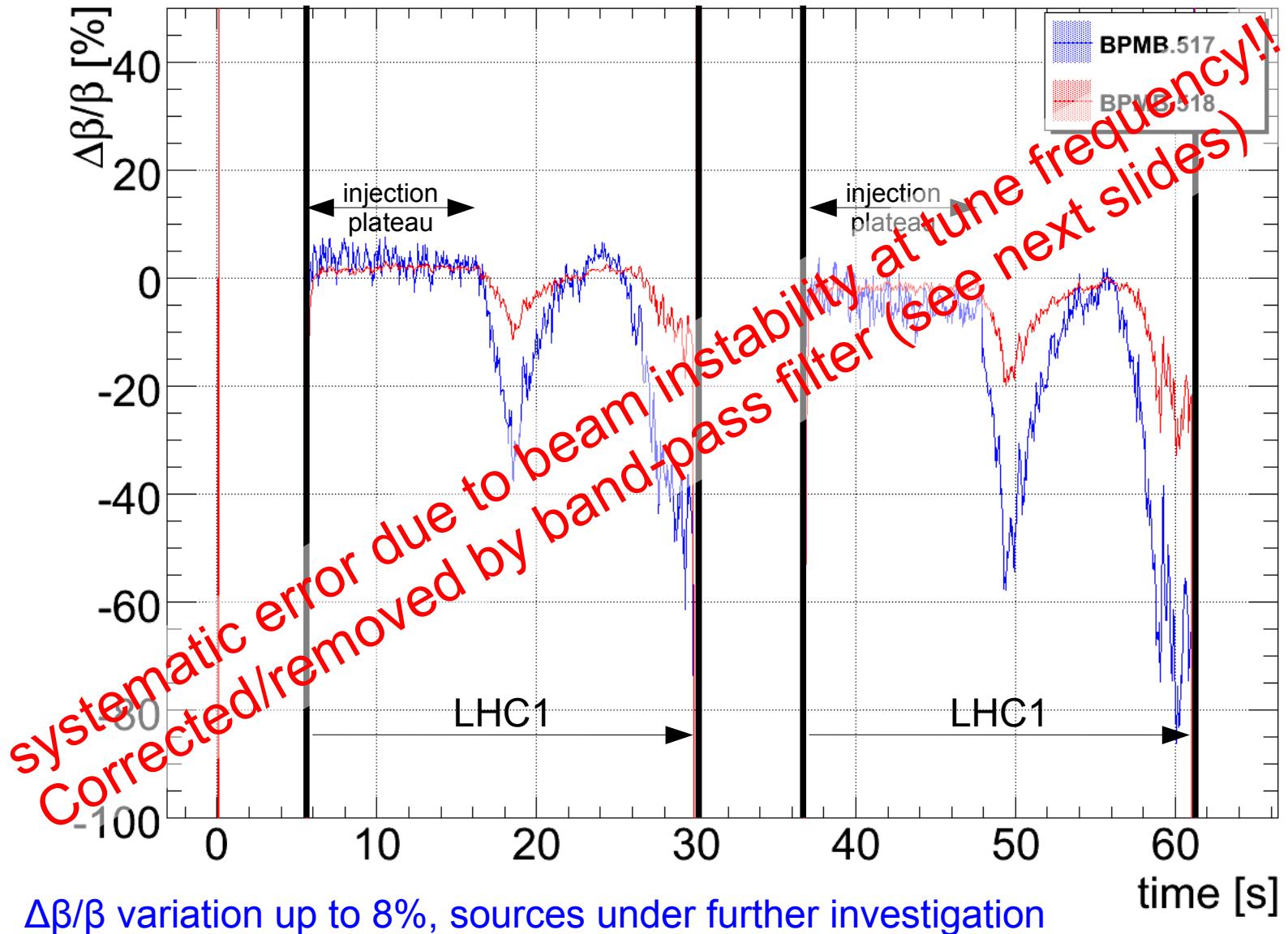
Further Exploitation Possibilities

- System can be further exploited for fast and transparent measurements of physics affecting $\Delta\beta/\beta$ that earlier required significant amount of beam time
- Example: vertical off-momentum β -Beat:
 - Continuous radial modulation: $\Delta p/p \approx 1 \cdot 10^{-3}$ @ 1 Hz
 - One full measurement data set every second!
 - N.B. Step in phase → off-centre horizontal orbit in lattice sextupoles



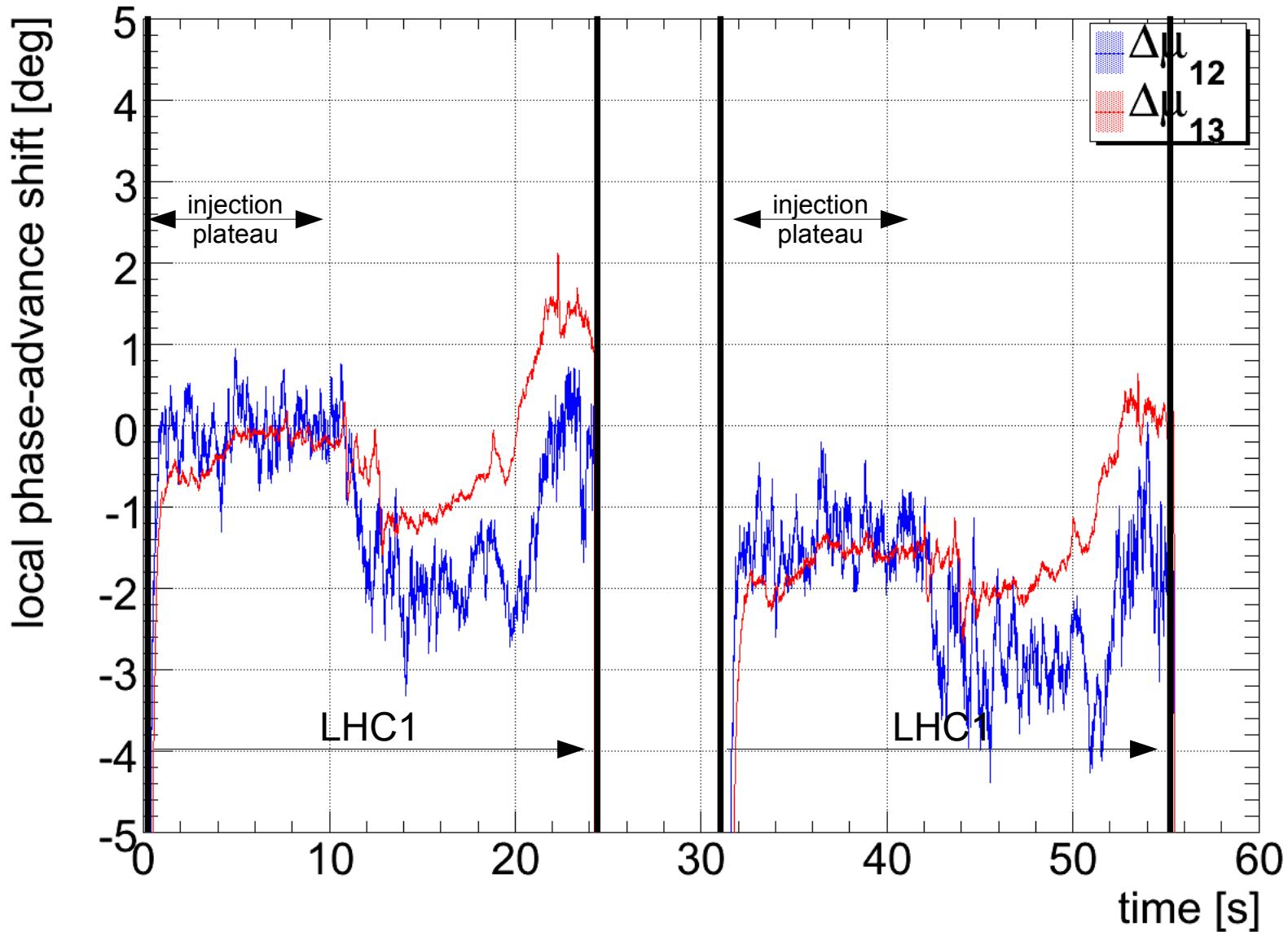
Example: SPS LHC1 cycle-to-cycle beta-beat

- In between two coasts...



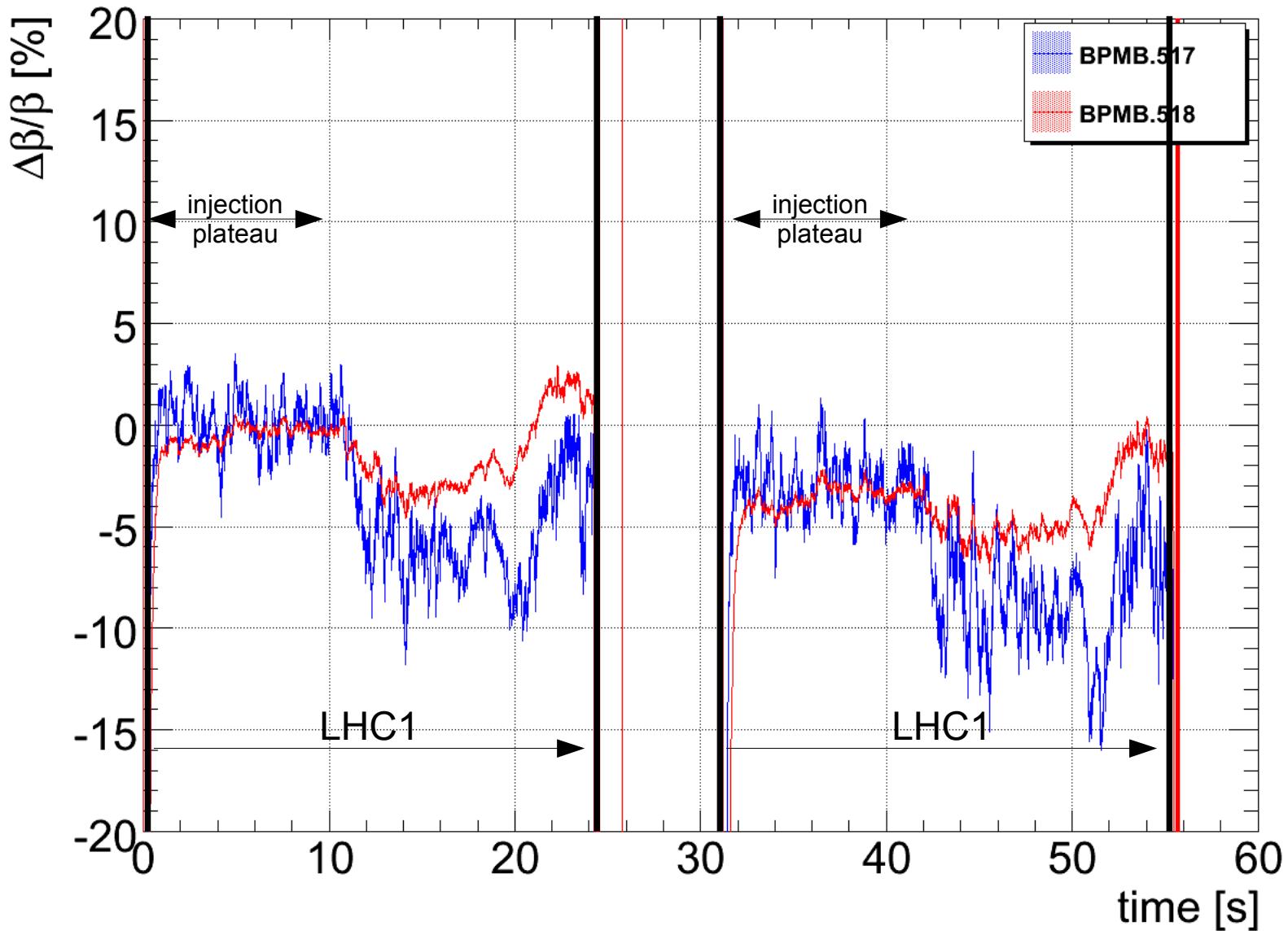
Example: SPS LHC1 cycle-to-cycle phase-beat

- In between two coasts...



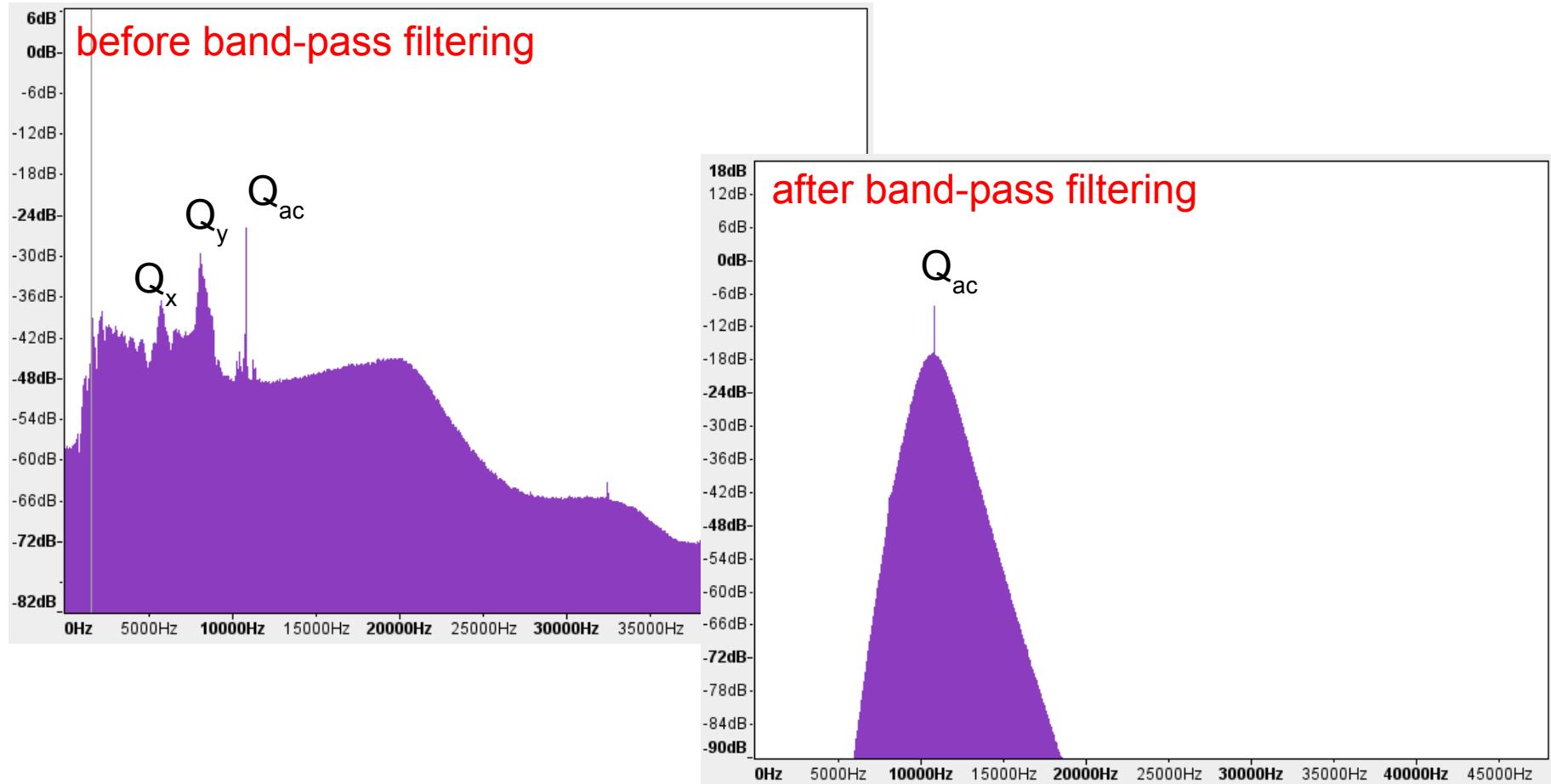
Example: SPS LHC1 cycle-to-cycle beta-beat

- In between two coasts...

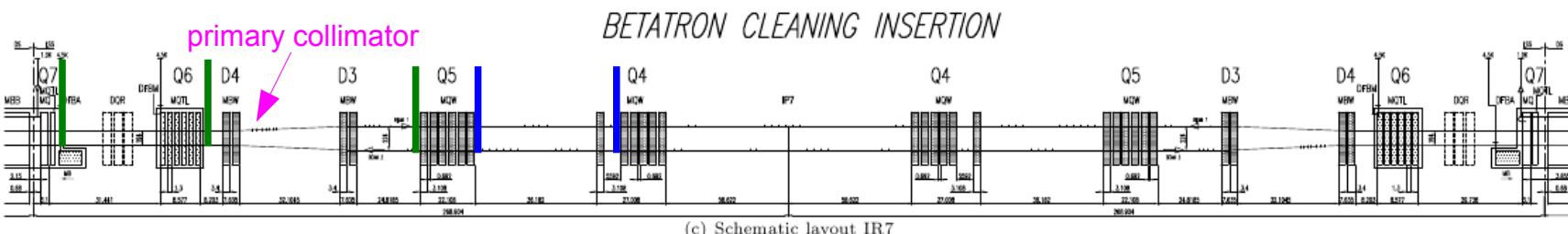


Example: SPS LHC1 cycle-to-cycle stability necessary correction

- Fourier Spectrum before and after band-pass filter (carrier at 10.8 kHz)



- Beside the intrinsic loss of signal due to the 3dB-signal splitter, initial tests show that sharing and cross-talk effects in been the regular WBTN and Beta-Beat system appears to be minimal.
 - tested with 75 ns/50 ns/25 ns/single nominal & pilot bunch configurations
 - 3dB-Splitter are being further tested in the lab using a bunch simulator setup
 - Affects mainly performance with ultra-low intensity bunches ($<2 \cdot 10^9$ p/bunch)
- Further Setup Improvement:
 - systematic drifts of analogue front-end stages $0.1^\circ/0.5$ hour (β^* meas)
 - Scalability and possible system integration (in view of LHC application)
 - Install 3 (+2) β -beat acquisition chains, both planes, either B1 or B2, in parallel to the regular BPM system, e.g. in LHC beta-cleaning insertion:



- the minimum installation without requiring to pull additional cables

The LHC Prototype system's usefulness is two-fold:

- Provided β does not change: study real beta-beat as a function of time and use measured values to possibly relax collimation requirements
- Provided β does change: same as above but – in addition – use real beta-beat values as an input to a real-time feedback loop (e.g. primary/secondary collimators, IPs)
 - Correction scheme similar to LHC Orbit FB system using the dispersion suppressor's and other individually powered quadrupoles
(N.B. we are not as “free” in correcting β as we are in correcting the orbit)

$$\frac{\vec{\Delta\beta}}{\beta} = \underline{R}_\beta \cdot \vec{\delta}_{DS} \xrightarrow{SVD} \vec{\delta}_{DS} = \underline{\tilde{R}}_\beta^{-1} \cdot \frac{\vec{\Delta\beta}}{\beta}$$

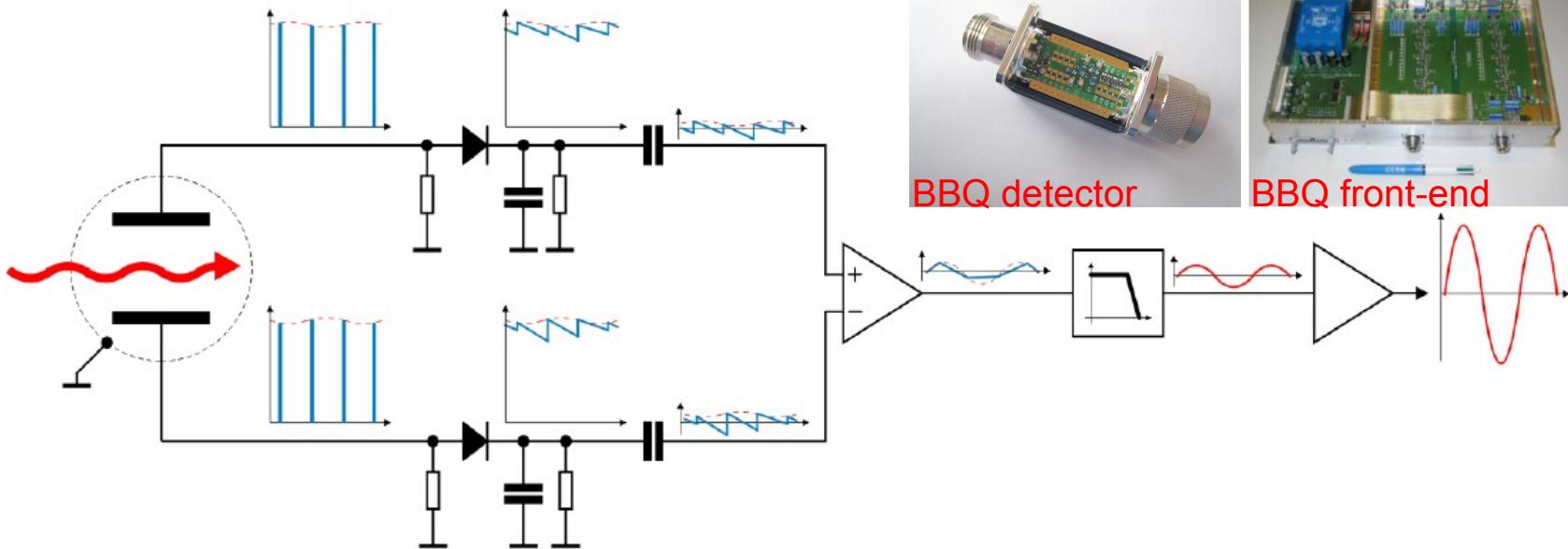
- Additional regions of interest: experimental insertions, Inj./Extr. IRs, ...
- The possible merit...
 - remove/reduce protection/cleaning limitations on β^* & stored intensity
 - +20% effective Luminosity

“Isn't this worth being further investigated?”

Conclusions

- A real-time β -beat measurement system has been successfully tested at the SPS based on the continuous measurement of the cell-to-cell phase advance.
 - Achieved resolution: $\Delta\beta/\beta < 1\% @ 1 \text{ Hz measurement bandwidth}$
 - Required S/N ratio: $\sim 20 \mu\text{m}/100 \text{ nm} \rightarrow \epsilon \text{ blow-up is a non-issue}$
 - compatible with nominal LHC operation
 - Shared pickup scheme (to 1st order) compatible with regular WBTN oper.
 - price of sharing: loose $\sim 3\text{dB}$ signal, OK for strip-line, buttons
 - may affect smallest detectable bunch intensity in IR7
- Measured residual 1% drift of SPS lattice and off-momentum beta-beat
- Present limitations of the system:
 - 45° optics (LHC arcs): $< 0.01^\circ \leftrightarrow \Delta\beta/\beta << 1\% @ 1\text{Hz bandwidth}$
 - residual beta-function stability and S/N ratio
 - Exp. Insertion optics: $\sim 0.1^\circ \leftrightarrow \Delta\beta/\beta \approx 30\% (\Delta\mu_{12} \approx 178^\circ)$
 - systematic phase and drifts, can be improved, target: $\Delta\beta/\beta_{IP} \approx 3\%$
- Provided your approval and support: We would like to install a similar setup in LHC-IR7 for 2009 to investigate residual drifts of the beta-function and possible exploitation of this measurement techniques within a real-time β -beat feedback loop

additional supporting slides



- Basic principle: AC-coupled peak detector
 - no saturation, self-triggered, no gain changes between pilot and nominal
 - intrinsically down samples spectra: ... 6 GHz → 1kHz ... f_{rev}
 - Base-band operation: very high sensitivity/resolution ADC available
 - Measured resolution estimate: < 10 nm → ε blow-up is a non-issue
- Since 2007: added low-pass filter in front of diodes to suppress intrinsic longitudinal (carrier) signal propagation into transverse oscillations

- Beta-Beat Sources
 - Quadrupole gradient and Momentum errors
 - Feed-down due to off-centre horizontal orbit in lattice sextupoles
 -
- Requirements: Brüning, Fartoukh, *LHC Project Report 501*

Peak hor. β -beating [%]	Mechanical aperture	14 / 15 (inj. / col.)
Peak vert. β -beating [%]	Mechanical aperture	16 / 19 (inj. / col.)
R.M.S. hor. β -beating [%]	Mechanical aperture	4.8 / 5.2 (inj. / col.)
R.M.S. vert.. β -beating [%]	Mechanical aperture	5.5 / 6.6 (inj. / col.)

- Effects on orbit, Energy, Tune, Q' and C⁻ can essentially cast into matrices:

$$\boxed{\Delta \vec{x}(t) = \underline{R} \cdot \vec{\delta}(t)} \quad \text{with} \quad R_{ij} = \frac{\sqrt{\beta_i \beta_j}}{\gamma \sin(\pi Q)} \cdot \cos(\Delta \mu_{ij} - \pi Q) + \frac{D_i D_j}{C(\alpha_c - 1/\gamma^2)}$$

matrix multiplication

- LHC matrices' dimensions:

$$\underline{R}_{\text{orbit}} \in \mathbb{R}^{1070 \times 530} \quad \underline{R}_Q \in \mathbb{R}^{2 \times 16} \quad \underline{R}_{Q'} \in \mathbb{R}^{2 \times 32} \quad \underline{R}_{C^-} \in \mathbb{R}^{2 \times 10/12}$$

- control consists essentially in inverting these matrices:

$$\left\| \vec{x}_{\text{ref}} - \vec{x}_{\text{actual}} \right\|_2 = \left\| \underline{R} \cdot \vec{\delta}_{ss} \right\|_2 < \epsilon \rightarrow \vec{\delta}_{ss} = \tilde{\underline{R}}^{-1} \Delta \vec{x}$$

- Some potential complications:
 - Singularities = over/under-constraint matrices, noise, element failures, spurious BPM offsets, calibrations, ...
 - Time dependence of total control loop → “The world goes SVD....”

Linear algebra theorem*:

$$\begin{matrix} n \times \text{cor. circuits} \\ \downarrow \end{matrix} \quad \boxed{\begin{matrix} R \\ m \times \text{observables} \end{matrix}} = \begin{matrix} U \\ \text{orthogonal columns} \end{matrix} \times \begin{matrix} \Lambda \\ \text{diagonal matrix} \end{matrix} \times \begin{matrix} V^T \\ \text{orthogonal rows} \end{matrix}$$

eigen-vector relation:

$$\lambda_i \vec{u}_i = \underline{R} \cdot \vec{v}_i$$

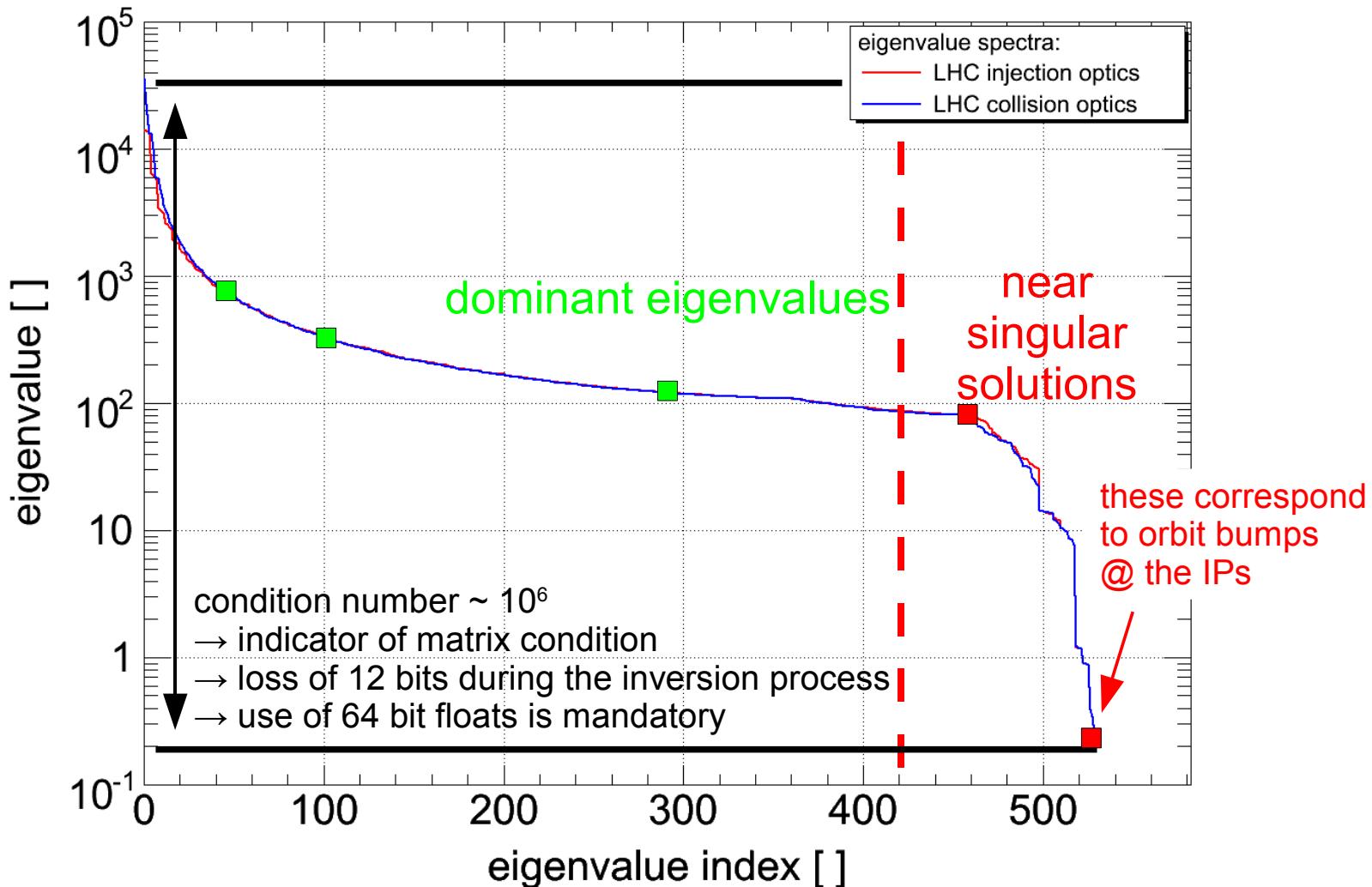
$$\lambda_i \vec{v}_i = \underline{R}^T \cdot \vec{u}_i$$

- though decomposition is numerically more complex final correction is a simple vector-matrix multiplication:

$$\vec{\delta}_{ss} = \tilde{R}^{-1} \cdot \Delta \vec{x} \quad \text{with} \quad \tilde{R}^{-1} = \underline{V} \cdot \underline{\Lambda}^{-1} \cdot \underline{U}^T \quad \Leftrightarrow \quad \vec{\delta}_{ss} = \sum_{i=0}^n \frac{a_i}{\lambda_i} \vec{v}_i \quad \text{with} \quad a_i = \vec{u}_i^T \Delta \vec{x}$$

- numerical robust, minimises parameter deviations Δx and circuit strengths δ
- Easy removal of singularities, (nearly) singular eigen-solutions have $\lambda_i \sim 0$
 - to remove those solution: if $\lambda_i \approx 0 \rightarrow 1/\lambda_i := 0'$
 - discarded eigenvalues corresponds to solution pattern unaffected by the FB

Eigenvalue spectra for vertical LHC response matrix using all BPMs and CODs:



- Optics imperfections may deteriorate the convergence speed but do not affect absolute convergence (response functions are 'monotonic'):
- Example: 2-dim orbit error surface projection

